

Solving Equations Using Factoring

a) Factored form:

1. $x(x+2)=0 \Rightarrow \{-2, 0\}$
2. $(x-3)(x+4)=0 \Rightarrow \{-4, 3\}$
3. $(2x-4)(5x+3)=0 \Rightarrow \{-3/5, 2\}$

b) Removing Common Factor:

1. $x^2 + 4x = 0 \Rightarrow x(x+4) = 0 \Rightarrow \{0, -4\}$
2. $4x^2 - 12x = 0 \Rightarrow 4x(x-3) = 0 \Rightarrow \{0, 3\}$
3. $x(x-1) + 9(x-1) = 0 \Rightarrow (x-1)(x+9) = 0 \Rightarrow \{-9, 1\}$ $x(x-1) + 9(x-1) = 0$

c) Difference of Squares:

1. $x^2 - 25 = 0 \Rightarrow (x+5)(x-5) = 0 \Rightarrow \{-5, 5\}$
2. $x^2 - 81 = 0 \Rightarrow (x+9)(x-9) = 0 \Rightarrow \{-9, 9\}$
3. $x^2 - 169 = 0 \Rightarrow (x+13)(x-13) = 0 \Rightarrow \{-13, 13\}$
4. $4x^2 - 25 = 0 \Rightarrow (2x+5)(2x-5) = 0 \Rightarrow \{-5/2, 5/2\}$
5. $36 - x^2 = 0 \Rightarrow -(x^2 - 36) = 0 \Rightarrow -(x+6)(x-6) = 0 \Rightarrow \{-6, 6\}$
6. $144 - 81x^2 = 0 \Rightarrow -(81x^2 - 144) = 0 \Rightarrow -9(3x+4)(3x-4) = 0 \Rightarrow \{-4/3, 4/3\}$
7. $3x^2 - 12 = 0 \Rightarrow 3(x+2)(x-2) = 0 \Rightarrow \{-2, 2\}$
8. $5x^2 - 45 = 0 \Rightarrow 5(x+3)(x-3) = 0 \Rightarrow \{-3, 3\}$

d) Easy Type 1

1. $x^2 + 7x + 12 = 0 \Rightarrow (x+4)(x+3) = 0 \Rightarrow \{-3, -4\}$
2. $x^2 + 15x + 16 = 0 \Rightarrow \text{prime}$
3. $x^2 + 15x + 56 = 0 \Rightarrow (x+8)(x+7) = 0 \Rightarrow \{-8, -7\}$
4. $x^2 + 14x = -40 \Rightarrow x^2 + 14x + 40 = 0 \Rightarrow (x+10)(x+4) = 0 \Rightarrow \{-10, -4\}$
5. $3x^2 + 60x + 225 = 0 \Rightarrow 3(x^2 + 20x + 75) = 0 \Rightarrow 3(x+15)(x+5) = 0 \Rightarrow \{-15, -5\}$

e) Easy Type 2

1. $x^2 - 12x + 13 = 0 \Rightarrow \text{can not factor}$
2. $x^2 - 15x + 14 = 0 \Rightarrow (x-14)(x-1) = 0 \Rightarrow \{1, 14\}$
3. $x^2 - 9x + 18 = 0 \Rightarrow (x-6)(x-3) = 0 \Rightarrow \{3, 6\}$

$$4. \quad x^2 - 13x = -30 \Rightarrow x^2 - 13x + 30 = 0 \Rightarrow (x-10)(x-3) = 0 \Rightarrow \{3,10\}$$

$$5. \quad 4x^2 - 20x = -16 \Rightarrow 4x^2 - 20x + 16 = 0 \Rightarrow 4(x^2 - 5x + 4) = 0 \Rightarrow \\ 4(x-4)(x-1) = 0 \Rightarrow \{1,4\}$$

f) Easy Type 3

$$1. \quad x^2 + 5x - 6 = 0 \Rightarrow (x+6)(x-1) = 0 \Rightarrow \{-6,1\}$$

$$2. \quad x^2 + 8x - 48 = 0 \Rightarrow (x+12)(x-4) = 0 \Rightarrow \{-12,4\}$$

$$3. \quad x^2 + 3x - 54 = 0 \Rightarrow (x+9)(x-6) = 0 \Rightarrow \{-9,6\}$$

$$4. \quad x^2 + 6x = 40 \Rightarrow x^2 + 6x - 40 = 0 \Rightarrow (x+10)(x-4) = 0 \Rightarrow \{-10,4\}$$

$$5. \quad 3x^2 + 15x - 18 = 0 \Rightarrow 3(x^2 + 5x - 6) = 0 \Rightarrow 3(x+6)(x-1) = 0 \Rightarrow \{-6,1\}$$

g) Easy Type 4

$$1. \quad x^2 - 7x - 8 = 0 \Rightarrow (x-8)(x+1) = 0 \Rightarrow \{-1,8\}$$

$$2. \quad x^2 - 12x - 28 = 0 \Rightarrow (x-14)(x+2) = 0 \Rightarrow \{-2,14\}$$

$$3. \quad x^2 - 5x - 36 = 0 \Rightarrow (x-9)(x+4) = 0 \Rightarrow \{-4,9\}$$

$$4. \quad x^2 - 3x = 88 \Rightarrow x^2 - 3x - 88 = 0 \Rightarrow (x-11)(x+8) = 0 \Rightarrow \{-8,11\}$$

$$5. \quad -4x^2 + 8x + 252 = 0 \Rightarrow -4(x^2 - 2x - 63) = 0 \Rightarrow -4(x-9)(x+7) = 0 \Rightarrow \{-7,9\}$$