

Radicals - Rules

1. No perfect n^{th} power under a radical

$$\sqrt{8} = \sqrt{2^3} = 2\sqrt{2}$$

$$\sqrt{x^3} = x\sqrt{x}$$

2. No fraction under a radical sign $\sqrt{\frac{1}{3}}$, $\sqrt{\frac{x}{y}}$

3. No radical in the den.

$$\frac{1}{\sqrt{3}}$$

$$\frac{2}{\sqrt{5}}$$

$$\frac{1}{\sqrt{3} + 1}$$

$$\frac{1}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}}$$

$$\frac{\sqrt{2}}{2}$$

$$\frac{3}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}}$$

$$\frac{3\sqrt{5}}{5}$$

$$\frac{2\sqrt{3}}{5\sqrt{7}} \cdot \frac{\sqrt{7}}{\sqrt{7}}$$

$$\frac{2\sqrt{21}}{5 \cdot 7}$$

$$\frac{6}{\sqrt{6}} = \frac{1 \cdot 3}{2 \cdot 3}$$

$$\frac{3}{\sqrt{6}} \cdot \frac{\sqrt{6}}{2}$$

$$3 \cdot \sqrt{5}$$

$$\sqrt{4} = 2$$

$$\sqrt{2^2} = 2$$

$$\sqrt{49} = 7$$

$$\sqrt{7^2} = 7$$

$$\sqrt{11^2} = 11$$

$$\sqrt{2} \cdot \sqrt{2} = \sqrt{2^2} = 2$$

$$\sqrt{11} \cdot \sqrt{11} = \sqrt{11^2} = 11$$

(radical x itself = the radicand)

$$\sqrt{23} \cdot \sqrt{23} =$$
$$\sqrt{x^2} \cdot \sqrt{x^2} = x^2$$

$$\frac{6}{5\sqrt{12}}$$

$2^2 \cdot 3$

$$\frac{6}{5\sqrt{2^2 \cdot 3}}$$

$$\frac{6}{5 \cdot 2\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}}$$

$$\frac{\cancel{2} \cdot 3}{5 \cdot \cancel{2} \sqrt{3}}$$

$$\frac{3}{5 \cdot \cancel{2} \cdot \cancel{2}} = \frac{\sqrt{3}}{5}$$

$$\frac{6}{5\sqrt{12}} \cdot \frac{\sqrt{12}}{\sqrt{12}}$$

$$\frac{6\sqrt{12}^{2^2-3}}{5 \cdot 12}$$

$$\frac{\cancel{2} \cdot 3}{5 \cdot \cancel{2} \cdot \sqrt{3}}$$

$$\frac{5 \cdot \cancel{2}}{\cancel{2} \cdot 3}$$

$$\frac{5\sqrt{6 \cdot 3}}{3\sqrt{2}} \cdot \frac{5\sqrt{3}}{3} = \frac{5\sqrt{2} \cdot \sqrt{3}}{3\sqrt{2}}$$

$$\frac{3\sqrt{20}}{2\sqrt{60}} = \frac{3\sqrt{2^2 \cdot 5}}{2\sqrt{2^2 \cdot 3 \cdot 5}} \quad \frac{2}{4} = \frac{1}{2}$$

$$= \frac{3}{2\sqrt{3}} \cdot \frac{\sqrt{3}}{3} = \frac{\cancel{3}\sqrt{3}}{2 \cdot \cancel{3}}$$

$$\frac{1}{(\sqrt{3}+1)} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{\sqrt{3}}{3+\sqrt{3}}$$

$$\frac{1}{(\sqrt{3}+1)} \cdot \frac{(\sqrt{3}+1)}{(\sqrt{3}+1)} = \frac{\sqrt{3}+1}{4+2\sqrt{3}}$$

$$\sqrt{3}(\sqrt{3}+1) + 1(\sqrt{3}+1)$$

$$\textcircled{3} + \sqrt{3} + \sqrt{3} + \textcircled{1}$$

$$4 + 2\sqrt{3}$$

$$\frac{1}{(\sqrt{3}+1)} \cdot \frac{(\sqrt{3}-1)}{(\sqrt{3}-1)} = \frac{\sqrt{3}-1}{2}$$

$$\sqrt{3}(\sqrt{3}-1) + 1(\sqrt{3}-1)$$

$$3 - \sqrt{3} + \sqrt{3} - 1$$

$$\underbrace{\hspace{10em}}$$

$$2$$

$$(x+2)(x-2) = x^2 - 4$$

Conjugate

NO middle

term if multiplied $x^2 + 4x + 4$

To multiply

1. 1ST x 1ST

2. Last x last

always separated by a minus

$$\rightarrow (x+2)^2$$

$$\rightarrow (x+2)(x+2)$$

$$\rightarrow (x-2)(x-2)$$

$$x^2 - 4x + 4$$

$$\rightarrow (x-2)^2$$

$$(3x-7)(3x+7) = 9x^2 - 49$$

$$(\sqrt{5}+2)(\sqrt{5}-2) = 5 - 4 = 1$$

$$(3\sqrt{2}+\sqrt{5})(3\sqrt{2}-\sqrt{5}) = 18 - 5 = 13$$

$$(5\sqrt{11} + \sqrt{13})(5\sqrt{11} - \sqrt{13})$$
$$275 - 13$$
$$\underline{262}$$
$$\begin{array}{r} 25 \\ 11 \\ \hline 25 \\ 25 \\ \hline 275 \end{array}$$

$$\frac{(3\sqrt{5} - 7)}{(6\sqrt{2} + \sqrt{3})} \cdot \frac{(6\sqrt{2} - \sqrt{3})}{(6\sqrt{2} - \sqrt{3})}$$

$$\frac{72 - 3}{69}$$

$$3\sqrt{5}(6\sqrt{2} - \sqrt{3}) - 7(6\sqrt{2} - \sqrt{3})$$
$$18\sqrt{10} - 3\sqrt{15} - 42\sqrt{2} + 7\sqrt{3}$$

$$\sqrt{\frac{3}{5}} = \frac{\sqrt{3}}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{\sqrt{15}}{5}$$

$$\sqrt{\frac{x}{y}} = \frac{\sqrt{x}}{\sqrt{y}} \cdot \frac{\sqrt{y}}{\sqrt{y}} = \frac{\sqrt{xy}}{y}$$