

Higher Order, Implicit Derivatives and Curve Sketching

A. Higher order derivatives: Determine the 1st and 2nd order derivatives for each of the following:

1. $f(x) = 5x^3 - 3x^5$

2. $f(x) = \frac{x^3 + 7}{x}$

3. $f(x) = \sin(x^2)$

B. Application:

A dynamite blast blows a heavy rock straight up with a launch velocity of 160 ft/sec. It reaches a height of $s(t) = 160t - 16t^2$ feet after t sec.

- How high does the rock go?
- What are the velocity and the speed of the rock when it is 256 feet above the ground on the way up? On the way down?
- What is the acceleration of the rock at any time t during its flight (after the blast)?
- When does the rock hit the ground?

C. Implicit Differentiation

1. $x^2y + xy^2 = 6$ with respect to x

2. $y^2 = x^2 + \sin xy$ with respect to x

3. $2xy + y^2 = x + y$ with respect to y

4. $2x^3 - 3y^2 = 8$ - find the 2nd derivatives

D. Application

Determine the equation of the line through the point (2, 3) tangent to the curve defined by the equation $x^2 + xy - y^2 = 1$

E. Curve Sketching

Sketch the curve $f(x) = 4x^2(1 - x^2)$